

EPFL

Duration: 120 minutes

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2025

SCIPER: **1000001** Room: **BCH 2201** Signature:

Wait for the start of the exam before turning to the next page. This booklet is printed double-sided, 24 pages. Do not unstaple or detach any pages.

Materials This is a closed-book exam. Paper documents and electronic devices are not allowed. Place your student ID and writing utensils on your desk. Place all other personal items at the front of the room. If you need additional draft paper, raise your hand and we will provide some. Time All points are not equal: exercises that have the same number of points may not be equally difficult. Look at the whole exam before starting. Appendix The last pages of this exam contain an appendix with useful function signatures. You may use functions from the Scala standard library even if they do not appear in the appendix. Use a pen To avoid scanning errors, only use black or blue pens for the MCQ part: no pencils! Use white corrector if necessary. **Grading scheme** The exam contains a total of 75 points. The points for each question are indicated next to it. Stay functional and Do not use vars, while loops, for...do loops, etc. (this will result in 0 points clean for that question). Points are attributed for correctness, succinctness, efficiency, and simplicity.

Respectez les consignes suiv	antes Read these guidelines Beachten Sie bitte	die unten stehenden Richtlinien
choisir une réponse select an answer Antwort auswählen	ne PAS choisir une réponse NOT select an answer NICHT Antwort auswählen	Corriger une réponse Correct an answer Antwort korrigieren
ce qu'il ne	aut <u>PAS</u> faire what should <u>NOT</u> be done was man <u>N</u>	ICHT tun sollte



1 Refactoring (6 pts)

Some or all the following snippets of code can be refactored using the List API. **Select which list function** is the **optimal** choice, if any. Then **write** the refactored version in the box. If none of the proposed choices work, check "None" and leave the box blank.

Choose only one option.

Question 1	(2 points)
0 1 2	Do not write here.
<pre>def example1(l: List[Int]): List[Int] = l match case Nil => Nil case head :: tail => head + 1 :: example1(tail)</pre>	<pre>def example1(l: List[Int]): List[Int] =</pre>
foldLeftfoldRightr	reduceLeft reduceRight map
Question 2	(2 points)
	Do not write here.
<pre>def example2(l: List[Int]): List[Int] = l match case Nil => Nil case head :: tail => if head % 2 == 0 then head :: example2(tail) else example2(tail)</pre>	<pre>def example2(l: List[Int]): List[Int] =</pre>
foldLeftfoldRightr	reduceLeft reduceRight map flatMap None
Question 3	(2 points)
0 1 2	Do not write here.
<pre>def example3(l: List[Int]): Boolean = l match case Nil => true case head :: tail => if head > 10 then true && example3(tail) else false && example3(tail)</pre>	<pre>def example3(l: List[Int]): Boolean =</pre>
foldLeftfoldRightr	reduceLeft reduceRight map flatMap None



2 Proof (8 pts)

All lemmas on this page hold for all types T and S; f of type T => S; x and y of type T; and lst1, lst2, xs, ys, zs of type List[T].

Your task is to prove MapAppend:

```
(MAPAPPEND) (lst1 ++ lst2).map(f) === lst1.map(f) ++ lst2.map(f)
```

The proof is done by induction on lst1. You are given the following lemmas:

```
(NILAPPEND) Nil ++ xs === xs
  (APPENDNIL) xs ++ Nil === xs

(CONSAPPEND) (x :: xs) ++ ys === x :: (xs ++ ys)

(APPENDCONS) xs ++ (y :: ys) === (xs ++ (y :: Nil)) ++ ys

(APPENDASSOC) xs ++ (ys ++ zs) === (xs ++ ys) ++ zs

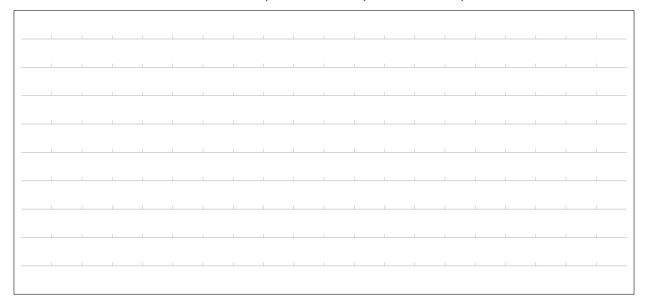
  (MapNil) Nil.map(f) === Nil

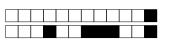
  (MapCons) (x :: xs).map(f) === f(x) :: xs.map(f)
```

Complete each case of the proof below by writing a sequence of equalities. Write every step of reasoning. For each step, you may only use one of the lemmas above or the induction hypothesis in the inductive case, and you must write the name of the lemma you are using. You do not need to use all of the given lemmas:

Base case: lst1 is Nil. Therefore, you need to prove:

(Nil ++ lst2).map(f) === Nil.map(f) ++ lst2.map(f)







Question 5 (5 points)

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Do not write here.

Inductive case: lst1 is x :: xs. Therefore, you need to prove:

$$((x :: xs) ++ lst2).map(f) === (x :: xs).map(f) ++ lst2.map(f)$$

given that the induction hypothesis, named IH, is true: for all ys of type ${\tt List[T]}$,

$$(xs ++ ys).map(f) === xs.map(f) ++ ys.map(f)$$

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3 Tree symmetry (18 pts)

In this exercise, you will work with binary trees, focusing on mirroring and symmetry.

Here is the structure that you will use throughout the exercise:

```
case class Tree[T](value: T, left: Option[Tree[T]], right: Option[Tree[T]])
def Leaf[T](value: T): Some[Tree[T]] = Some(Tree(value, None, None))
```

3.1 Mirroring trees (4 pts)

3.1.1 Definition

Given a two-dimensional picture, we can define its "vertical mirror image" by flipping it along a vertical axis, as in the example to the right.

We can perform a similar transformation on binary trees, producing a "vertical mirror tree". Below are two examples:



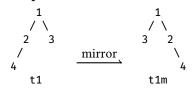


Example 0:



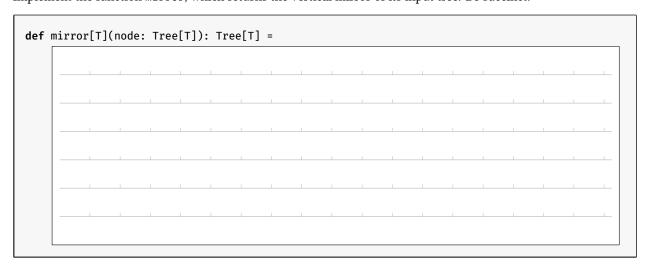
```
val t0 = Tree(1, Leaf(2), Leaf(3))
val t0m = Tree(1, Leaf(3), Leaf(2))
assertEquals(mirror(t0), t0m)
```

Example 1:



val t1 = Tree(1, Some(Tree(2, Leaf(4), None)), Leaf(3))
val t1m = Tree(1, Leaf(3), Some(Tree(2, None, Leaf(4))))
assertEquals(mirror(t1), t1m)

Implement the function mirror, which returns the vertical mirror of its input tree. Be succinct.





3.2 Tree symmetry (14 pts)

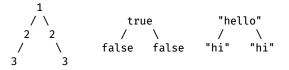
3.2.1 Definition

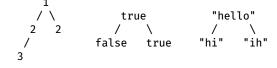
A two-dimension drawing can have "vertical symmetry". For example, the three pictures on the left are vertically symmetric, whereas the three pictures on the right are not:





We can define a similar notion on trees. The three trees on the left are symmetric, whereas the three trees on the right are not:





You are given the following definitions:

- The *children* of a tree are the **non-None** subtrees among left and right. Each tree has 0, 1, or 2 children.
- The descendants of a tree are its children, plus their children, and so on, recursively.

You are also given the following functions:

```
// Returns the size of a tree
def size[T](tree: Tree[T]): Int =
    val l = tree.left.map(size).getOrElse(0)
    val r = tree.right.map(size).getOrElse(0)
    1 + l + r

// Returns the in-order traversal of a tree
def inOrder[T](tree: Tree[T]): Seq[T] =
    val l = tree.left.map(inOrder).getOrElse(Seq.empty)
    val r = tree.right.map(inOrder).getOrElse(Seq.empty)
    (l :+ tree.value) ++ r

// Returns the set of elements in the tree
def elements[T](tree: Tree[T]): Set[T] =
    inOrder(tree).toSet
```

3.2.2 Part 1: Counterexamples

The following definition of a symmetric tree is **wrong**:

"A tree is symmetric if and only the following property is true for it and all of its descendants: 'I have no children, or all of my children are of the same size and contain the same set of elements'."

The following counterexamples show that this definition is incorrect:

Counterexample 0.1: false negative (symmetric tree, incorrectly rejected)

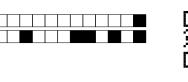


Counterexample 0.2: false positive (non-symmetric tree, incorrectly accepted)





Question 7	(1 point)
	Do not write here.
Counterexample 0.2 above is not <i>minimal</i> : there are smaller trees that show that definition 0 is wrong.	Counterexample:
Draw a <i>minimal false positive</i> (a minimal non-symmetric tree that this definition accepts) in the box to the right.	
Question 8	(2 points)
	Do not write here.
The following definition of a symmetric tree is wrong :	Counterexample:
"A tree is symmetric if and only if its children are all equal."	
Draw a <i>minimal false negative</i> (a minimal symmetric tree that this definition does not accept) in the box to the right.	
Question 9	(2 points)
0 1 2	Do not write here.
The following definition of a symmetric tree is wrong :	Counterexample:
"A tree is symmetric if and only if it has no children or all of its children are symmetric."	
Draw a <i>minimal false positive</i> (a minimal non-symmetric tree that this definition accepts) in the box to the right.	
Question 10	(2 points)
	Do not write here.
The following definition of a symmetric tree is wrong :	Counterexample:
"A tree is symmetric if and only if it has no children, or if it has two children and both of them are symmetric."	
Draw a <i>minimal false positive</i> (a minimal non-symmetric tree that this def-	





Question 11	(2 points)
0 1 2	Do not write here.
The following definition may be correct or incorrect:	Counterexample:
"A tree is symmetric if and only if it is equal to its vertical mirro (as defined in the previous exercise)."	or
Indicate whether it is correct or not. If it is incorrect, draw a recounterexample in the box to the right.	ninimal
Correct Incorrect	
Question 12	(2 points)
0 1 2	Do not write here.
The following definition may be correct or incorrect:	Counterexample:
"A tree is symmetric if and only if an in-order traversal produce a palindromic sequence (i.e. a sequence that reads the same for wards and backward, for example "4, 5, 1, 5, 4")."	I
Indicate whether it is correct or not. If it is incorrect, draw a recounterexample in the box to the right.	ninimal
Correct Incorrect	
3.2.3 Part 2: Executable specifications	
Question 13	(3 points)
0 1 2 3	Do not write here.
Write the function isSymmetric so that it returns true if and only You may use the functions defined in the previous part. Be succinct def isSymmetric[T](tree: Tree[T]): Boolean =	



Variance (5 pts)

Question 14 (2 points)

The following code snippet has a variance error, and will be rejected by the Scala compiler:

```
4  trait I[+T]:
5  def t: T
6  def f(t: T): T
```

Select the error message that best describes the problem:

Construct a small program which would fail (throw an exception or crash) at runtime if the Scala compiler were to accept the trait definition above. In other words, show a program that would go wrong if variance checks were disabled for the trait definition above. **Keep your solution succinct.**

Your answer may only use usual constructions and applications of Scala functions and values; the types Int, String, Boolean, and Any, and their methods; and new classes defined by you that implement the trait I.

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5 Parallelism and complexity (14 pts)

In this section, we will use the .par method on collections to perform computations in parallel (this method becomes available after importing scala.collection.parallel.CollectionConverters.*).

5.1 Word statistics (6 pts)

In this exercise, you will compute statistics for very large sequences of words. To improve performance, we use the parallel aggregate function. This function first folds across contiguous subsequences of the input using seqop, then combines the results with combop.

```
abstract class ParSeq[+A] extends Seq[A]:
   // Aggregates the results of applying an operator to subsequent elements.
   def aggregate[B](z: => B)(seqop: (B, A) => B, combop: (B, B) => B): B
```

You are asked to complete the invocations by providing the body of seq or comb. Keep your code succinct.

Example task: Count the number of words in a sentence.

Solution:

```
def countWords(words: Seq[String]): Int =
  def seq(count: Int, word: String) = count + 1
  def comb(c1: Int, c2: Int) = c1 + c2
  words.par.aggregate(0)(seq, comb)
```

Task: Count how many words are considered "special" based on the given predicate. For example, the following test should pass:

```
test("wordstats: countSpecial"):
  val s = List("I", "love", "Scala", "so", "much")
  assertEquals(countSpecial(s, _.length == 4), 2)
  assertEquals(countSpecial(s, _.startsWith("t")), 0)
```

Complete the seq function below:





Question 17 (4 points)



Do not write here.

Task: Compute the frequency of each word, ignoring case differences. For example, the following test should pass:

```
test("wordstats: freqs"):
  val s = List("To", "be", "or", "not", "to", "be")
  assertEquals(freqs(s), Map("to" -> 2, "be" -> 2, "or" -> 1, "not" -> 1))
```

Complete the comb function below.

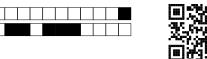


5.2 Complexity (8 pts)

Your are given the following definition of the Boid class and functions.

```
// You can assume that `Vector2(x:Float, y:Float)` supports addition to and
// subtraction from a `Vector2`, multiplication and division by a `Float`, and
// the `norm: Float` method. Calling `.sum` on a sequence of `Vector2` works
// as expected, using the `+` method.
case class Boid(position: Vector2, velocity: Vector2)
// Compute the avoidance force from other boids to this boid
def avoidanceForcePar(thisBoid: Boid, otherBoids: Vector[Boid]): Vector2 =
  otherBoids.par
                                                              // [1]
    .map(b => thisBoid.position + b.position)
    .map(diff => diff / 2)
// Compute the cohesion force from other boids to this boid
def cohesionForcePar(thisBoid: Boid, otherBoids: Vector[Boid]): Vector2 =
  otherBoids.par.map(_.position).sum
                                                              // [2]
                                                              // [3]
    / (otherBoids.par.length.toFloat + 1)
    - thisBoid.position
// Tick a boid, compute its next position and velocity using cohesion and avoidance forces
def tickBoidPar(thisBoid: Boid, allBoids: Vector[Boid]): Boid =
  val acc = avoidanceForcePar(thisBoid, allBoids) +
    cohesionForcePar(thisBoid, allBoids)
  Boid(
    thisBoid.position + thisBoid.velocity,
    thisBoid.velocity + acc
  )
// Tick all boids
def tickWorld(allBoids: Vector[Boid]): Vector[Boid] =
  allBoids.par.map(boid => tickBoidPar(boid, allBoids)).seq // [4]
```

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Question 20 (3 points)

A senior developer looked at this code and said:

"Those pars! They hurt my eyes! Get rid of as many of them as possible without impacting performance too badly for our average customer."

The average customer has a classic computer with 10 threads and runs the simulation with 1000 boids.

Check as many .par as possible that can be removed together without badly impacting performance.

	Remove	.par	number	1	(in	avoidance	eForce)		
	Remove	.par	number	2	(in	cohesion	force,	before	.map)
	Remove	.par	number	3	(in	cohesion	force,	before	.length)
	Remove	.par	number	4	(in	tickWorld	1)		



Campus renovation (23 pts)

EPFL is planning a major renovation of its campus. The goal is to maximize available classroom seating capacity while keeping a tight budget.

Definitions

We model the problem as follows:

- A campus plan is a two-dimensional grid of size (xSize, ySize) with a collection of buildings.
- A coordinate (x, y) defines a specific cell in the grid. Both x and y must be non-negative.

(0, 1) (1, 1) (2, 1) (3, 1) (4, 1)	(0, 0)	(1, 0)	(2, 0)	(3, 0)	(4, 0)	
(0, 0) (1, 0) (0, 0) (2, 0) (4, 0)	(0, 1)	(1, 1)	(2, 1)	(3, 1)	(4, 1)	
(0, 2) $(1, 2)$ $(2, 2)$ $(3, 2)$ $(4, 2)$	(0, 2)	(1, 2)	(2, 2)	(3, 2)	(4, 2)	

A building is described by:

- id: its identifier, for example "single deck";
- coords: the cells that it occupies in the campus, stored as a (non-empty) set of coordinates;
- price: its (non-negative) price in Swiss Francs;
- seats: the total number of seats provided by its classrooms.

In the following, we use the words "campus", "plan" and "campus plan" interchangeably.

In the diagram below, we illustrate an empty campus of size (3, 4) along with five buildings of various shapes and sizes.



Buildings 🎡 and 🟢 each occupy two coordinates; building 🕍 and 🕮 each occupy three coordinates; building 📳 occupies six coordinates.

Note that some buildings are disconnected (is one such example).

6.2 **Problem statement**

The aim of this exercise is to find a *feasible* campus plan that maximizes seating capacity.

- A plan is feasible when it is affordable and valid.
 - A plan is *affordable* if the total cost of the buildings is at most a given budget.
 - A plan is valid if it has no overlapping buildings and no buildings that extend out of campus bounds.
 - * Two buildings *overlap* if they have at least one coordinate in common.
 - * A building *extends out of the campus* if one of its coordinates is not within campus boundaries.

Here are some examples:

Building a extends out of campus bounds



Buildings 🏠 and 🛄 overlap (at (2, 0))



Valid plan

Valid plan



We define the following classes to reason about the campus renovation. You can assume that the methods defined here are correct and you are free to use them.

```
case class Coord(x: Int, y: Int):
  require(x >= 0 && y >= 0)
  // Component-wise addition: (1,2) + (3,4) = (4,6)
  def +(other: Coord): Coord = Coord(x + other.x, y + other.y)
```

```
case class CampusPlan(buildings: List[Building], xSize: Int, ySize: Int):
   // Return the same campus with the given building added
   def :+(b: Building): CampusPlan =
      require(b.fits(this))
      copy(buildings = b :: buildings)
```

```
case class Building(id: String, coords: Set[Coord], price: Int, seats: Int):
  // Checks that this building does not extend out of bounds of the campus
  def inBoundaries(c: CampusPlan): Boolean = // ...
```

Keep your code short and simple.

6.3 Fitting and translating (8 pts)

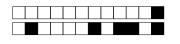
Question 21

Question 21

Do not write here.

A building b *fits* within a valid campus c if c :+ b is valid; that is, if the campus remains valid after adding the building to it. Write an extension method fits of Building such that b.fits(c) returns whether b fits in c. You may assume that c is valid.

```
extension (b: Building)
def fits(c: CampusPlan): Boolean =
```

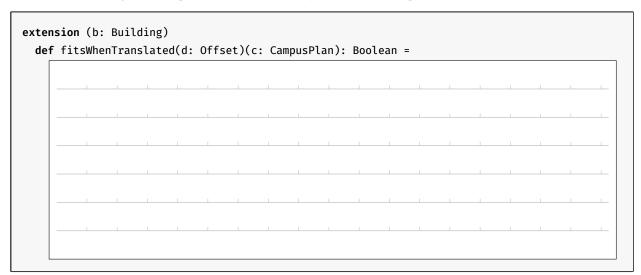




For the next two methods, we define Offset as:

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Write an extension method fitsWhenTranslated of Building such that b.fitsWhenTranslated(d)(c) returns true if and only if b fits in campus c when translated by d, as defined in question 21.

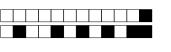






6.4 Find the best լ	plan (15 pts))
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7 Putting it all together (1 pt)

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Appendix

```
abstract class List[+A]:
  // Returns a new sequence containing the elements from the left hand operand
 // followed by the elements from the right hand operand.
 def ++[B >: A](suffix: IterableOnce[B]): List[B]
  // A copy of the list with an element prepended.
 def +:[B >: A](elem: B): List[B]
  // A copy of this sequence with an element appended.
 def :+[B >: A](elem: B): List[B]
  // Adds an element at the beginning of this list.
 def ::[B >: A](elem: B): List[B]
 // Selects all the elements of this sequence ignoring the duplicates.
 def distinct: List[A]
  // Selects all elements except the first n ones
 def drop(n: Int): List[A]
  // Tests whether a predicate holds for at least one element of this list.
 def exists(p: A => Boolean): Boolean
  // Selects all elements of this list which satisfy a predicate.
 def filter(p: A => Boolean): List[A]
  // Finds the first element of the list satisfying a predicate, if any.
 def find(p: A => Boolean): Option[A]
 // Builds a new list by applying a function to all elements of this list and
 // using the elements of the resulting collections.
 def flatMap[B](f: A => IterableOnce[B]): List[B]
  // Applies the given binary operator op to the given initial value z and all
 // elements of this sequence, going left to right. Returns the initial value
 // if this sequence is empty.
 def foldLeft[B](z: B)(op: (B, A) \Rightarrow B): B
  // Applies the given binary operator op to all elements of this list and the
 // given initial value z, going right to left. Returns the initial value if
  // this list is empty.
 def foldRight[B](z: B)(op: (A, B) => B): B
  // Tests whether a predicate holds for all elements of this list.
 def forall(p: A => Boolean): Boolean
  // Partitions this iterable collection into a map of iterable collections
  // according to some discriminator function.
 def groupBy[K](f: A => K): Map[K, List[A]]
  // The initial part of the collection without its last element.
 def init: List[A]
  // Iterates over the inits of this iterable collection.
 def inits: Iterator[List[A]]
  // Selects the last element.
 def last: A
  // Optionally selects the last element.
 def lastOption: Option[A]
  // Builds a new list by applying a function to all elements of this list.
 def map[B](f: A => B): List[B]
  // Applies the given binary operator op to all elements of this collection.
 def reduce[B >: A](op: (B, B) => B): B
 // Applies the given binary operator op to all elements of this collection,
  // going left to right.
  def reduceLeft[B >: A](op: (B, A) => B): B
```





```
// Applies the given binary operator op to all elements of this collection,
// going right to left.
def reduceRight[B >: A](op: (A, B) => B): B
// Returns a new list with the elements of this list in reverse order.
def reverse: List[A]
// Selects an interval of elements.
def slice(from: Int, until: Int): List[A]
// Sorts this sequence according to a comparison function.
def sortWith(lt: (A, A) => Boolean): List[A]
// Sums the elements of this list.
// You do not need to provide the num parameter explicitly.
def sum[B >: Int](implicit num: Numeric[B]): B
// Iterates over the tails of this sequence.
def tails: Iterator[List[A]]
// Selects the first n elements.
def take(n: Int): List[A]
// Converts this collection to a Set.
def toSet[B >: A]: Set[B]
// Returns a iterable collection formed from this iterable collection and
// another iterable collection by combining corresponding elements in pairs.
def zip[B](that: IterableOnce[B]): List[(A, B)]
// ...
```

```
abstract class Map[K, +V]:
 // Creates a new map obtained by updating this map with a given key/value pair.
 def +[V1 >: V](kv: (K, V1)): Map[K, V1]
 def updated[V1 >: V](key: K, value: V1): Map[K, V1]
 // Removes a key from this map, returning a new map.
 def -(key: K): Map[K, V]
  // Tests whether this map contains a binding for a key.
 def contains(key: K): Boolean
 // Applies the given binary operator op to the given initial value z
  // and all elements of this collection, going left to right.
 def foldLeft[B](z: B)(op: (B, (K, V)) \Rightarrow B): B
  // Optionally returns the value associated with a key.
 def get(key: K): Option[V]
 // Returns the value associated with a key, or a default value if the key is
  // not contained in the map.
 def getOrElse[V1 >: V](key: K, default: => V1): V1
 // Builds a new iterable collection by applying a function to all elements of
 // this iterable collection.
 def map[B](f: ((K, V)) => B): Iterable[B]
 // Builds a new map by applying a function to all elements of this map.
 def map[K2, V2](f: ((K, V)) => (K2, V2)): Map[K2, V2]
  // Converts this collection to a List.
 def toList: List[(K, V)]
  // ...
```





```
// Other functions
// Computes `a` and `b` in parallel and returns their results as a tuple
def parallel[A, B](a: => A, b: => B): (A, B) = ???

extension (that: Int)

// An immutable range from `that` up to but not including `end`
def until(end: Int): Range = ???

// An immutable range from `that` up to and including `end`
def to(end: Int): Range = ???
```

```
// Vector has the same methods as `List`, with the input and output types
// appropriately changed from `List[_]` to `Vector[_]`.
abstract class Vector[+A]
```

```
// Seq has the same methods as `List`, with the input and output types
// appropriately changed from `List[_]` to `Seq[_]`.
abstract class Seq[+A]
```

```
abstract class Set[A]:
  // Creates a new set with an additional element, unless the element is already present.
 def +(elem: A): Set[A]
  // Returns a new iterable collection containing the elements from the left
  // hand operand followed by the elements from the right hand operand.
 def ++[B >: A](suffix: IterableOnce[B]): Set[B]
  // Creates a new set with a given element removed from this set.
 def -(elem: A): Set[A]
 // Creates a new immutable set from this immutable set by removing all
  // elements of another collection.
 def --(that: IterableOnce[A]): Set[A]
  // Computes the difference of this set and another set.
 def diff(that: Set[A]): Set[A]
  // Tests whether a predicate holds for at least one element of this collection.
 def exists(p: A => Boolean): Boolean
  // Selects all elements of this iterable collection which satisfy a predicate.
 def filter(pred: A => Boolean): Set[A]
  // Builds a new iterable collection by applying a function to all elements of
  // this iterable collection and using the elements of the resulting collections.
 def flatMap[B](f: A => IterableOnce[B]): Set[B]
 // Tests whether a predicate holds for all elements of this collection.
 def forall(p: A => Boolean): Boolean
 // Partitions this iterable collection into a map of iterable collections
 // according to some discriminator function.
 def groupBy[K](f: A => K): Map[K, Set[A]]
  // Computes the intersection between this set and another set.
 def intersect(that: Set[A]): Set[A]
  // Returns true if this set is empty
  def isEmpty: Boolean
```



```
// Returns true if this set contains at least one element
def nonEmpty: Boolean
// Builds a new iterable collection by applying a function to all elements of
// this iterable collection.
def map[B](f: A => B): Set[B]
// Finds the maximum element of this set as measured by the given function.
// You do not need to provide the ord parameter explicitly.
def maxBy[B](f: A => B)(implicit ord: Ordering[B]): A
// Applies the given binary operator op to all elements of this collection.
def reduce[B >: A](op: (B, B) => B): B
// Tests whether this set is a subset of another set.
def subsetOf(that: Set[A]): Boolean
// An iterator over all subsets of this set.
def subsets(): Iterator[Set[A]]
// Converts this collection to a List.
def toList: List[A]
// ...
```

```
abstract class String:
  // Returns a new string containing the chars from this string followed by the
 // chars from the right hand operand.
 def +(suffix: IterableOnce[Char]): String
  // The rest of the string without its n first chars.
 def drop(n: Int): String
  // Tests if this string ends with the specified suffix.
 def endsWith(suffix: String): Boolean
 // Selects all chars of this string which satisfy a predicate.
 def filter(pred: Char => Boolean): String
 // Builds a new string by applying a function to all chars of this string and
 // using the elements of the resulting strings.
 def flatMap(f: Char => String): String
  // Tests whether a predicate holds for all chars of this string.
 def forall(p: Char => Boolean): Boolean
  // Optionally selects the first char.
 def headOption: Option[Char]
  // The initial part of the string without its last char.
 def init: String
  // Iterates over the inits of this string.
 def inits: Iterator[String]
  // Selects the last char of this string.
 def last: Char
  // Optionally selects the last char.
 def lastOption: Option[Char]
  // Builds a new collection by applying a function to all chars of this string.
 def map[B](f: Char => B): IndexedSeq[B]
 // Builds a new string by applying a function to all chars of this string.
 def map(f: Char => Char): String
  // Returns new sequence with elements in reversed order.
 def reverse: String
```





```
// Selects an interval of elements.
def slice(from: Int, until: Int): String
// Tests if this string starts with the specified prefix.
def startsWith(prefix: String): Boolean
// Returns a string that is a substring of this string.
def substring(beginIndex: Int, endIndex: Int): String
// Iterates over the tails of this string.
def tails: Iterator[String]
// A string containing the first n chars of this string.
def take(n: Int): String
// ...
```

```
abstract class Option[+A]:
 // Returns the value if the option is nonempty, otherwise returns the
 // given default value.
 def getOrElse[B >: A](default: => B): B
 // Returns true if the option is nonempty and the predicate holds for its
  // value.
 def exists(p: A => Boolean): Boolean
 // Returns true if the option is empty or the predicate holds for its value.
 def forall(p: A => Boolean): Boolean
 // Returns a new option containing the result of applying f to this option's
 // value if it is nonempty. Otherwise, returns None.
 def flatMap[B](f: A => Option[B]): Option[B]
 // Returns the value if the option is nonempty. Otherwise, throws
 // java.util.NoSuchElementException.
 def get: A
  // Returns true if this option is an instance of Some.
 def isDefined: Boolean
 // Returns true if this option is an instance of None.
 def isEmpty: Boolean
 // Applies the given function if this option is nonempty.
 def map[B](f: A => B): Option[B]
  // ...
```